

# Radar observations of sub-mesoscale fronts in the equatorial Pacific

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17 May 2022

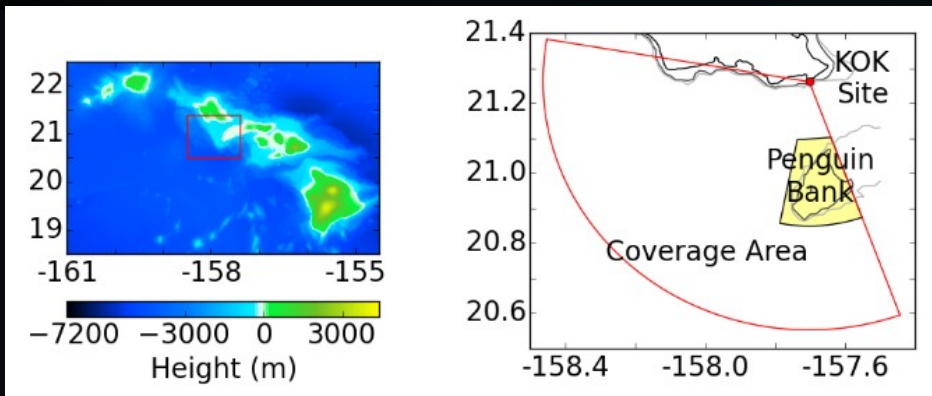


# Agenda

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- Misadventures in meteotsunamis
- Radar obs of sub-mesoscale fronts
  - Tropical instability vortices
  - Sub-mesoscale fronts
  - Cross-front differences
  - Conclusions

# 2011 Tōhoku tsunami

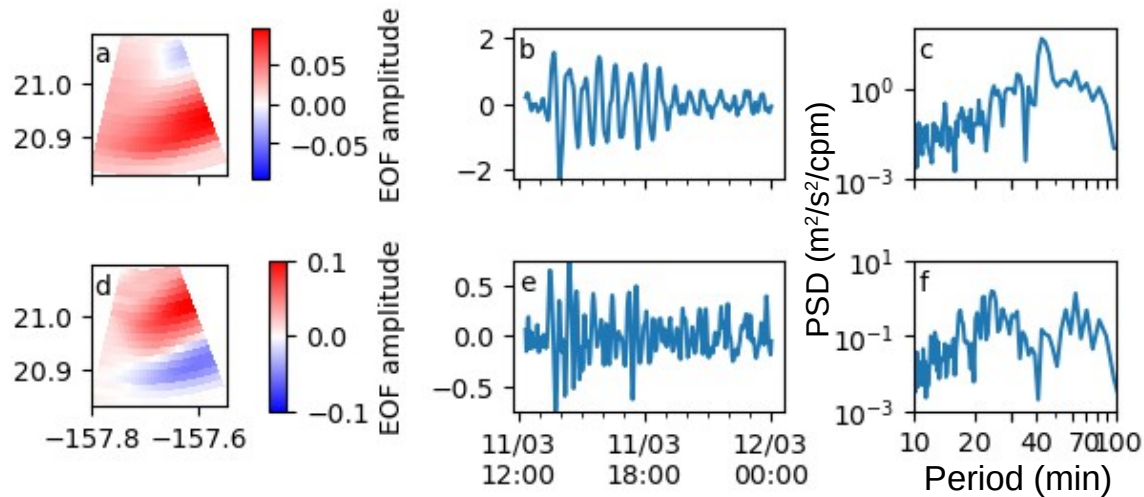


Moment magnitude 9.0

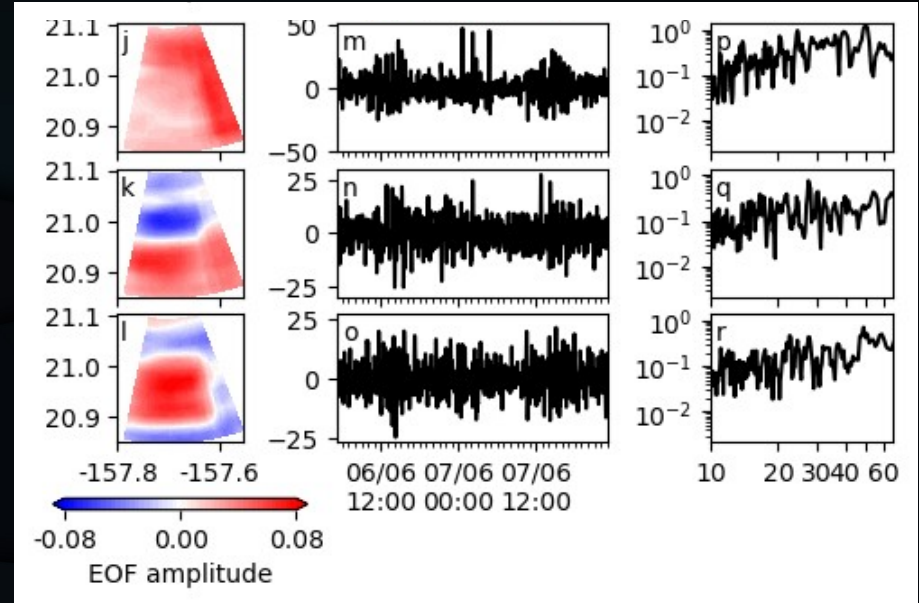
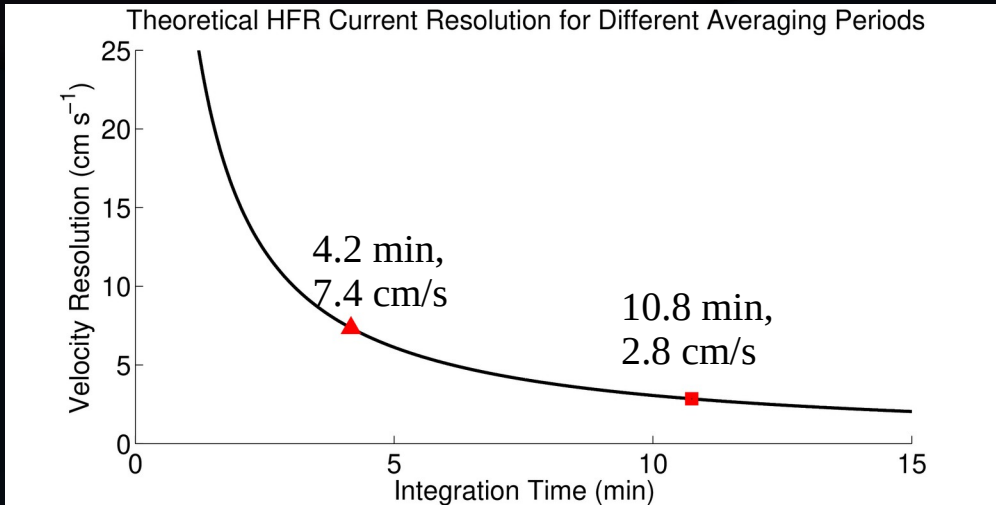
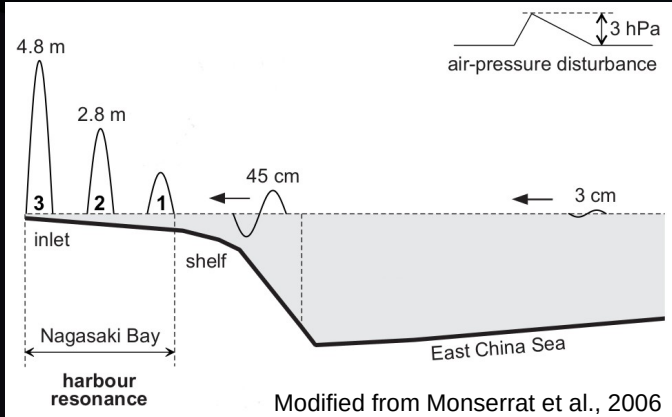
Arrived 1300 UTC on 11 March 2011

Asymmetrical expression  
on Penguin Bank

Well-defined arrival and  
subsequent oscillations



# Meteotsunamis in Hawaii



Some elements of resonance modes found, but not a complete suite of expected features

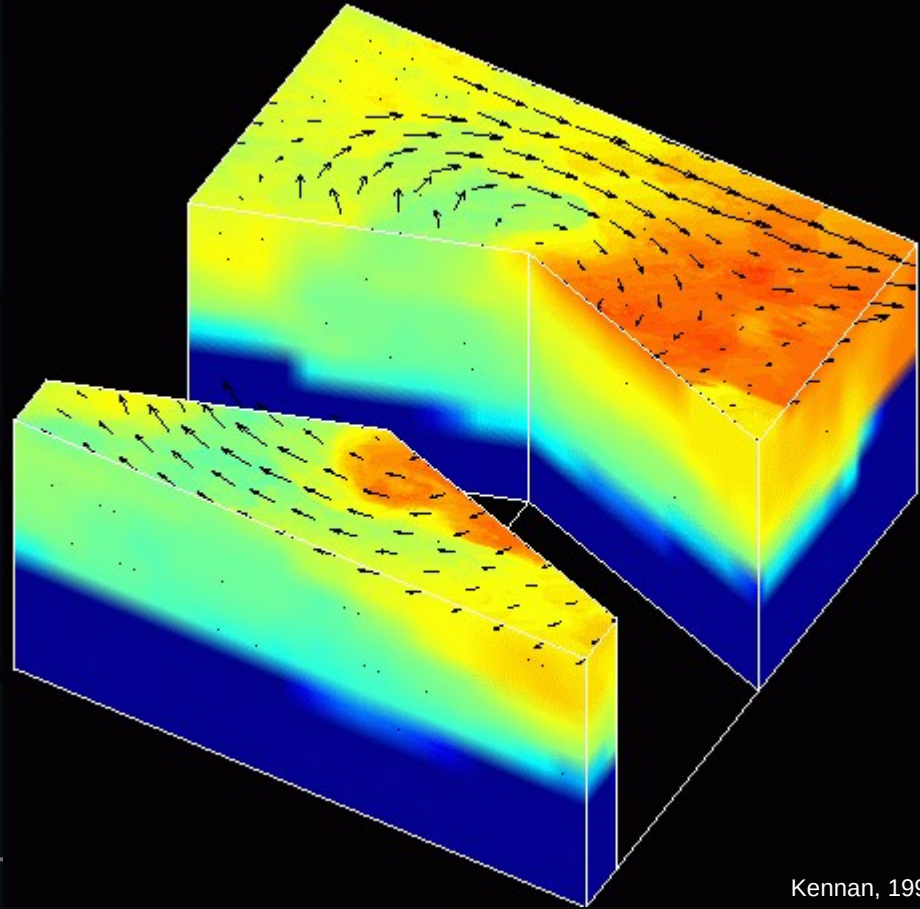


# Conclusions

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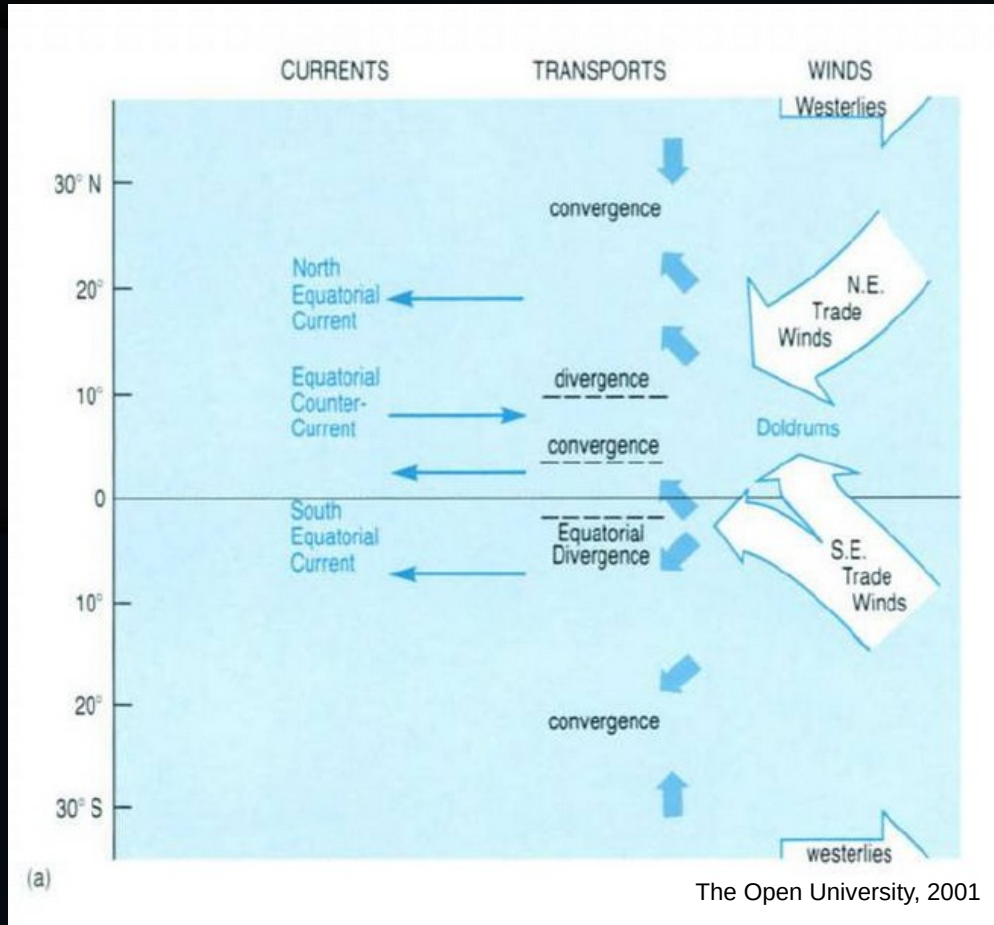
- Tsunamis arriving in Hawaii excite resonance modes that depend on local bathymetry and coastlines
- Meteotsunamis may occur in Hawaii, but they would be rare; if any occurred, resultant resonance excitation was too weak for HFDR detection
- In-situ instruments could detect resonance excitation from meteotsunamis

# Tropical instability vortices

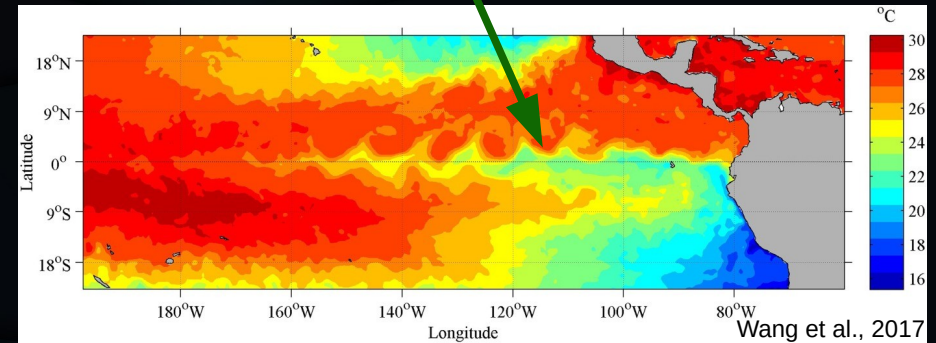


Kennan, 1996

# Equatorial Pacific



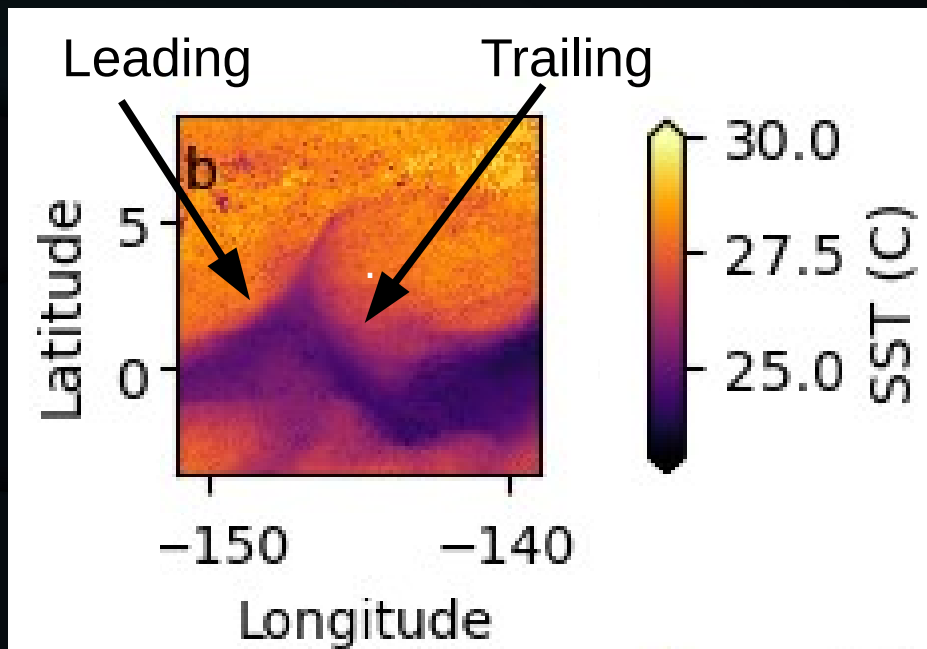
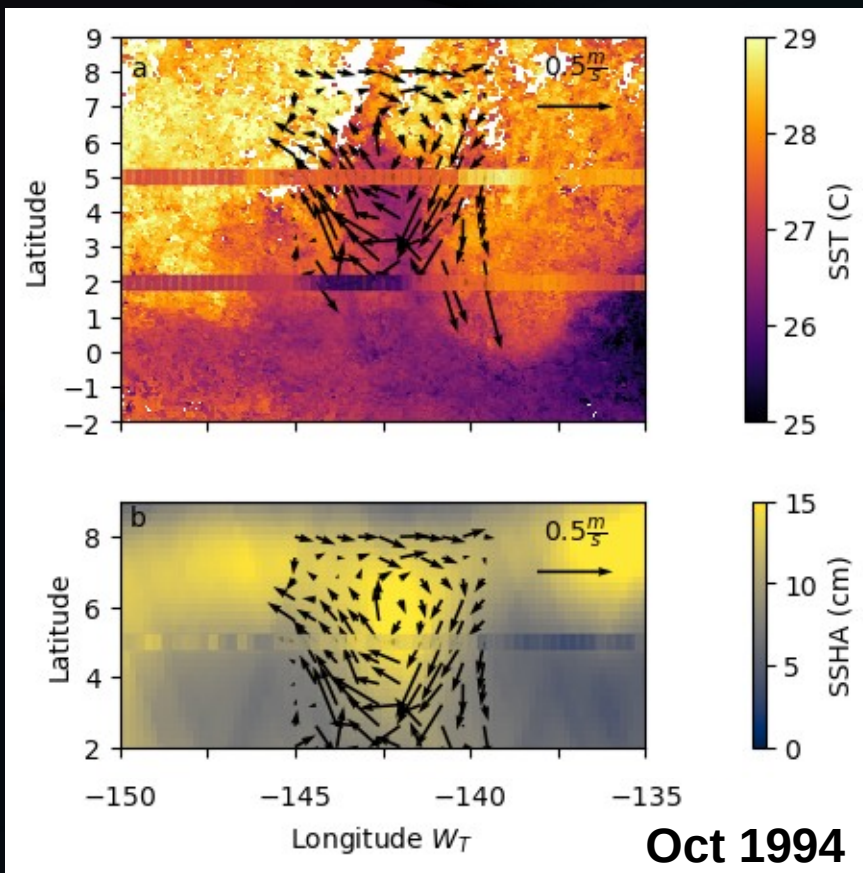
Trade winds  
↓  
Equatorial divergence  
↓  
Upwelling of cold, salty water  
↓  
North Equatorial Front



Zonal system of currents with shears  
↓  
Tropical instability vortices

# Tropical instability vortices

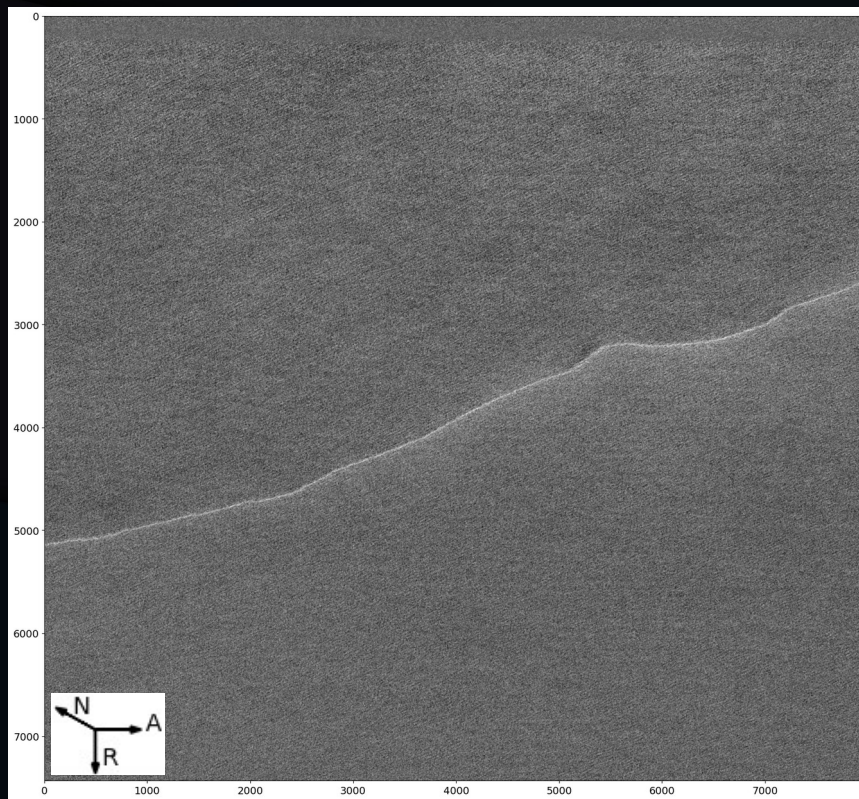
Translating frame of reference



2016  
to  
2019



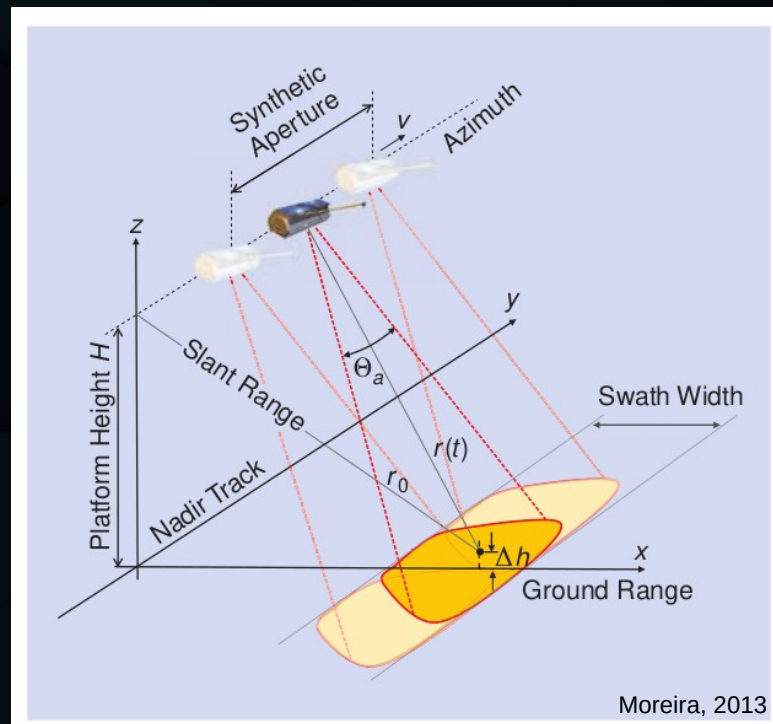
# Synthetic aperture radar



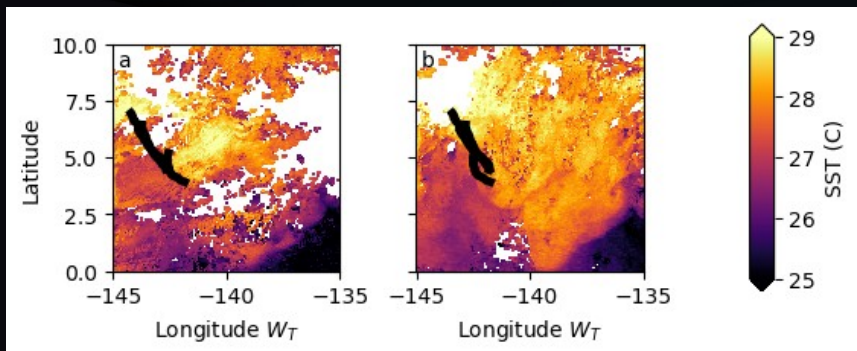
Oct 1994

Surface roughness on 3-30 cm scales

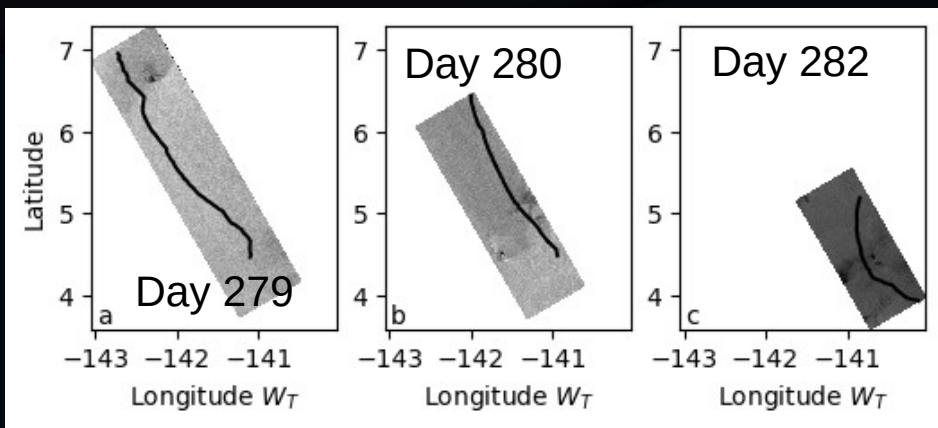
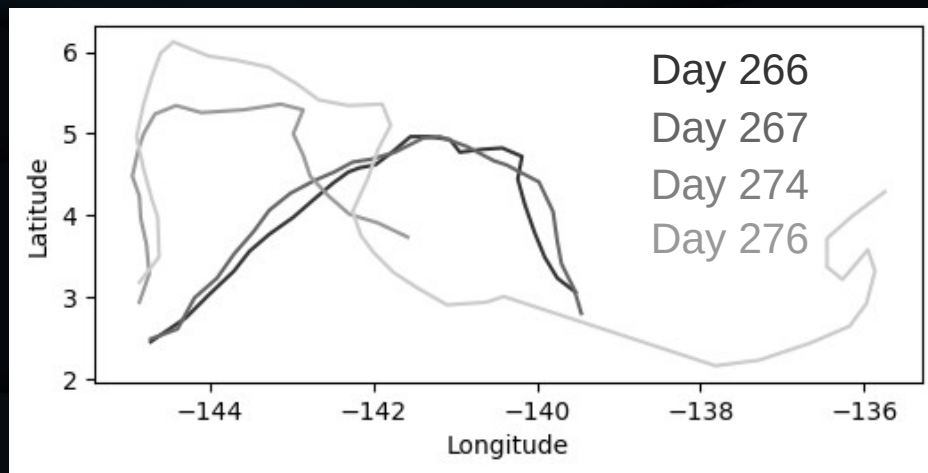
Convergence  $\Rightarrow$  wave breaking



# Swirling currents



Oct 1994

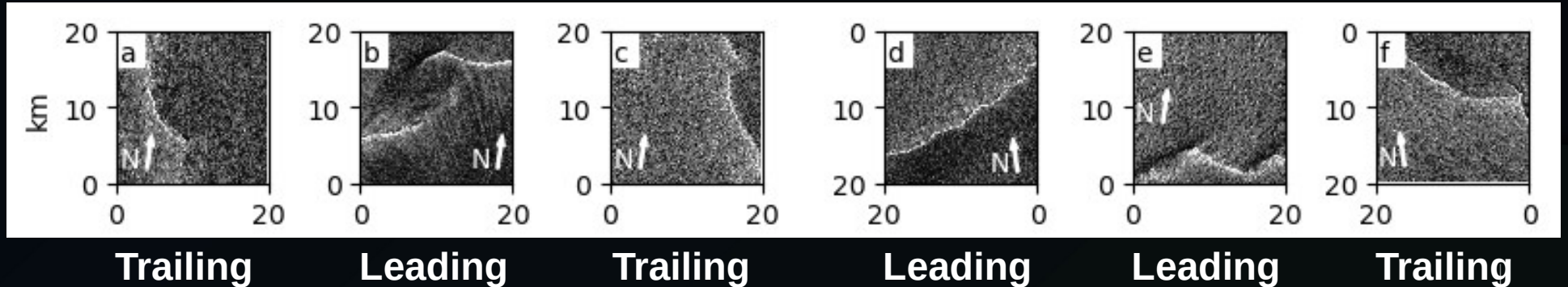
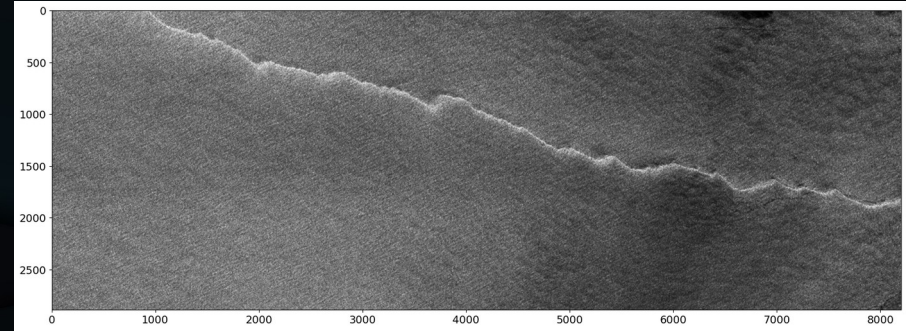
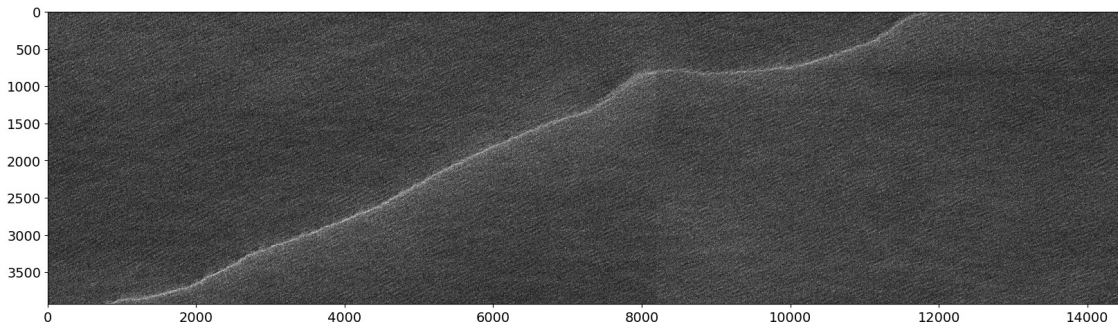


# SAR instabilities

Trailing – day 279

Oct 1994

Trailing – day 282



2016 to 2019



# Potential vorticity

$$q = \vec{\omega} \cdot \nabla b = (f + \zeta)N^2 + \vec{\omega}_h \cdot \nabla_h b$$

Potential vorticity

Buoyancy gradient

Vertical vorticity

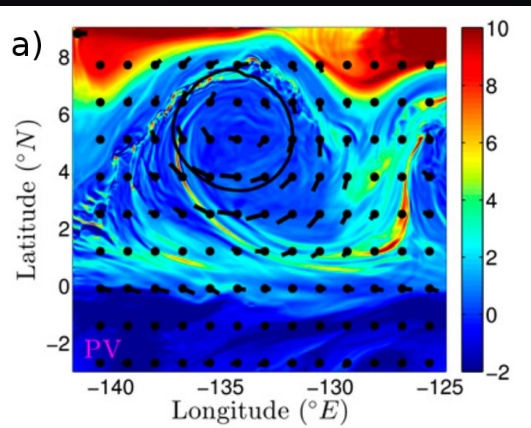
Horizontal vorticity

Total vorticity

Coriolis frequency

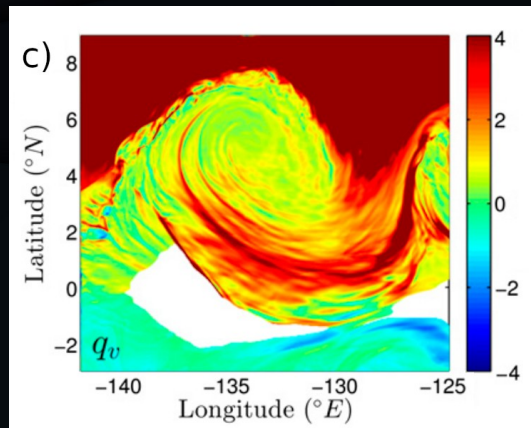
Buoyancy frequency

Horizontal buoyancy gradient



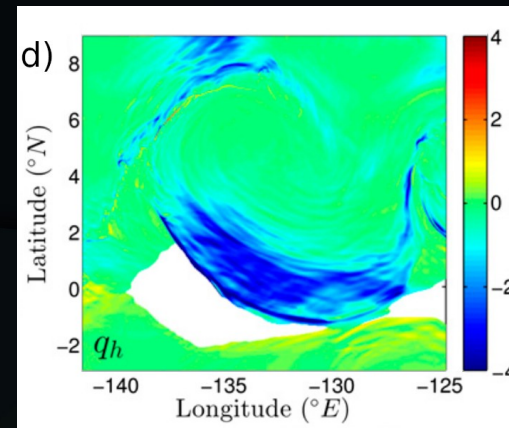
$q$

=



$q_v$

+



$q_h$



# Instability types

**Gravitational instability:**  
Heavy over light

$$N^2 < 0$$

$$q < 0$$

**Inertial instability:**  
Strong shear

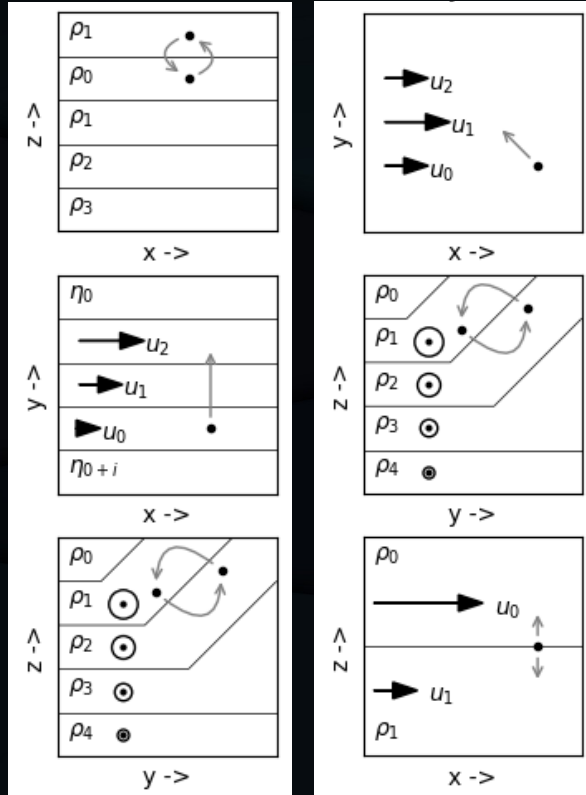
$$\partial u / \partial y > f$$

$$q < 0$$

**Symmetric instability:**  
Strong thermal wind

$$N^2 / |\partial u / \partial z|^2 < f / (\zeta + f)$$

$$q < 0$$



**Barotropic instability:**

Specific shear

$\partial q_v / \partial y$  changes sign

**ML baroclinic instability:**

Specific horizontal or vertical shear

$\partial q / \partial y$  changes sign

$\partial q / \partial y$  &  $\partial u / \partial z$  are:

same sign @ bottom  
opposite sign @ top

**Kelvin-Helmholtz instability:**

Strong shear

$$N^2 / |\partial u / \partial z|^2 < 1/4$$

# Instability types

~~Gravitational instability:  
Heavy over light~~

~~$$N^2 < 0$$~~

~~$$q < 0$$~~

~~Inertial instability:~~

~~Strong shear~~

**FOR  
FRONTAL  
SCALES**

~~$$\partial u / \partial y > f$$~~

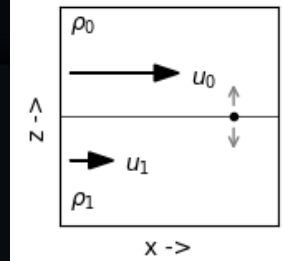
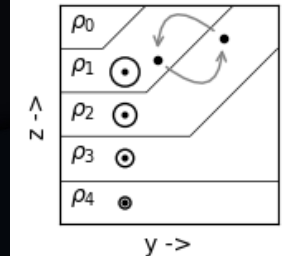
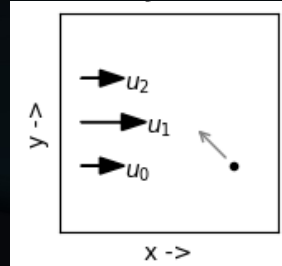
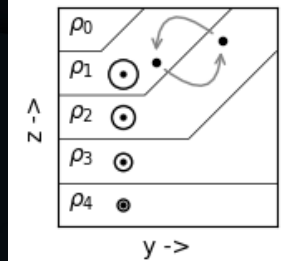
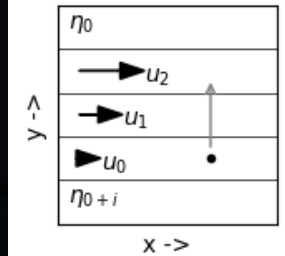
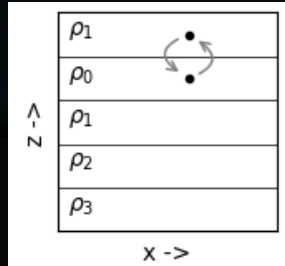
~~$$q < 0$$~~

~~Symmetric instability:~~

~~Strong thermal wind~~

~~$$N^2 / |\partial u / \partial z|^2 < f / (\zeta + f)$$~~

~~$$q < 0$$~~



**Barotropic instability:**

Specific shear

$\partial q_v / \partial y$  changes sign

**ML baroclinic instability:**

Specific horizontal or vertical shear

$\partial q / \partial y$  changes sign

$\partial q / \partial y$  &  $\partial u / \partial z$  are:

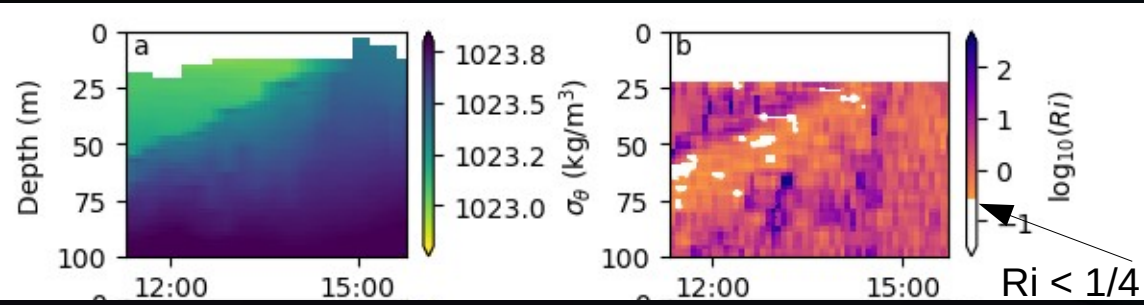
same sign @ bottom  
opposite sign @ top

**Kelvin-Helmholtz instability:**

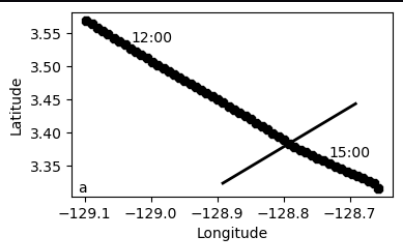
Strong shear

$$N^2 / |\partial u / \partial z|^2 < 1/4$$

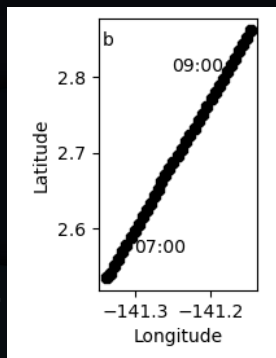
# Richardson numbers



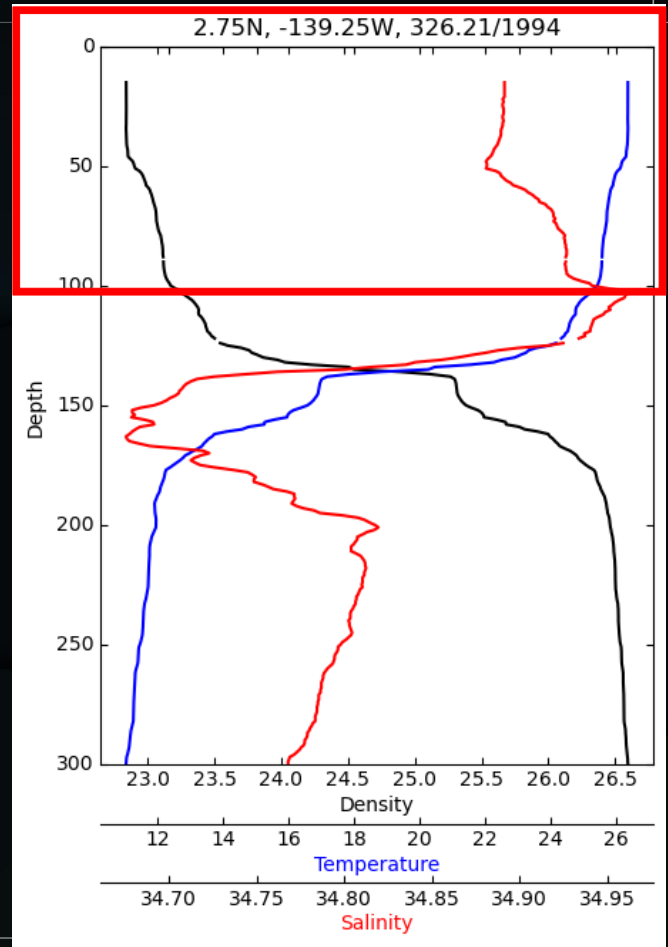
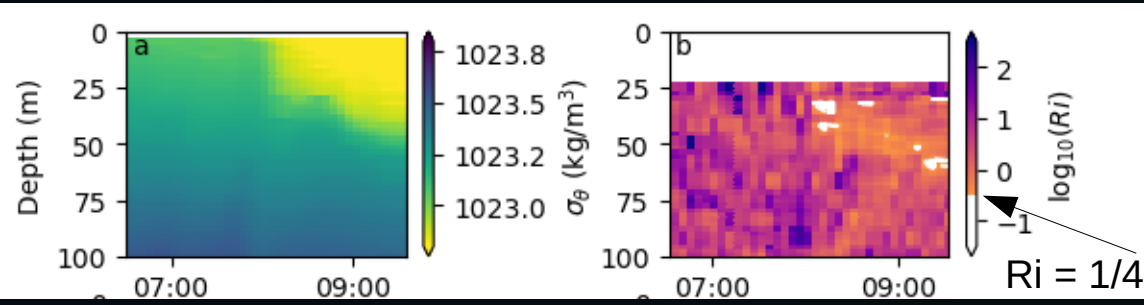
Only this in panels



Leading front  
Aug 1990



Trailing front  
Nov 1990



# Conclusions

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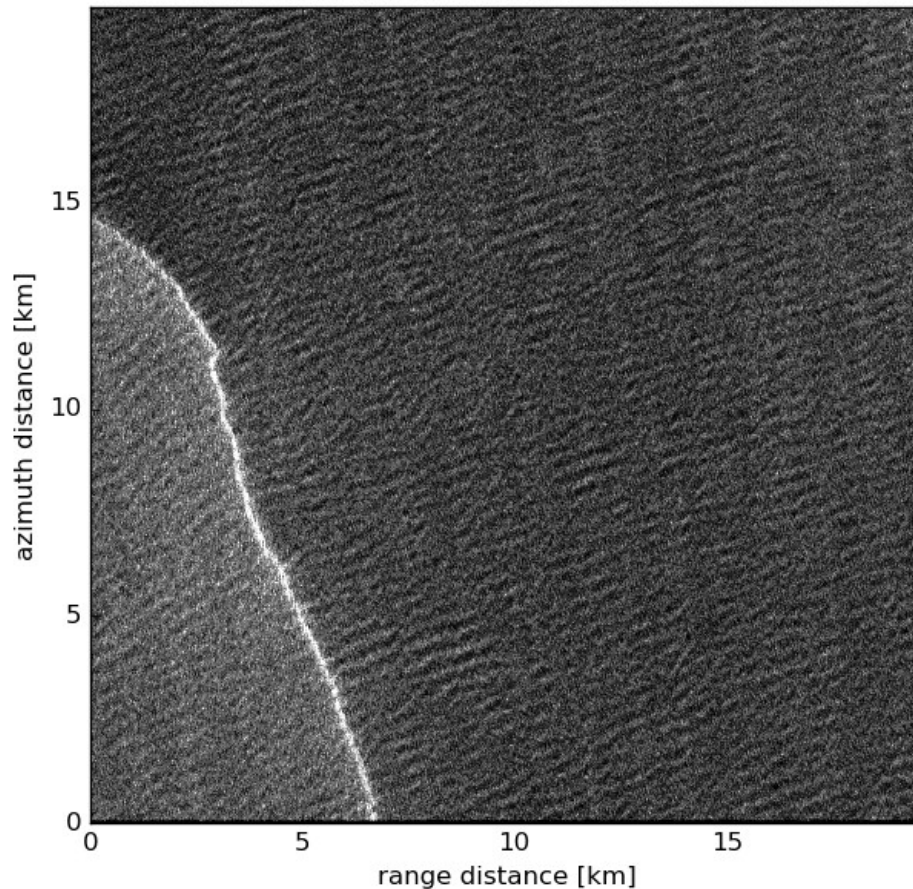
- Swirling currents advect, rotate, and deform SST fronts and trigger small-scale waves, cusps, and breaks
- Leading and trailing fronts are not subject to negative-PV instabilities, but instead to barotropic and mixed layer baroclinic instabilities
- Kelvin-Helmholtz instability may play a role in frontal dynamics



# Cross-front differences

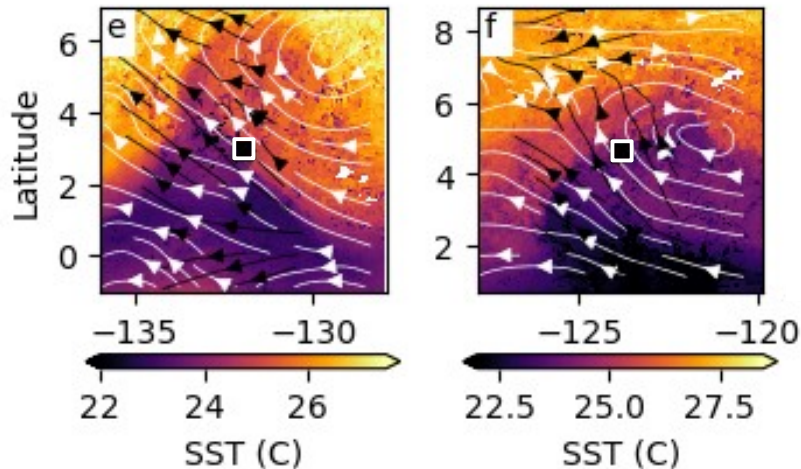
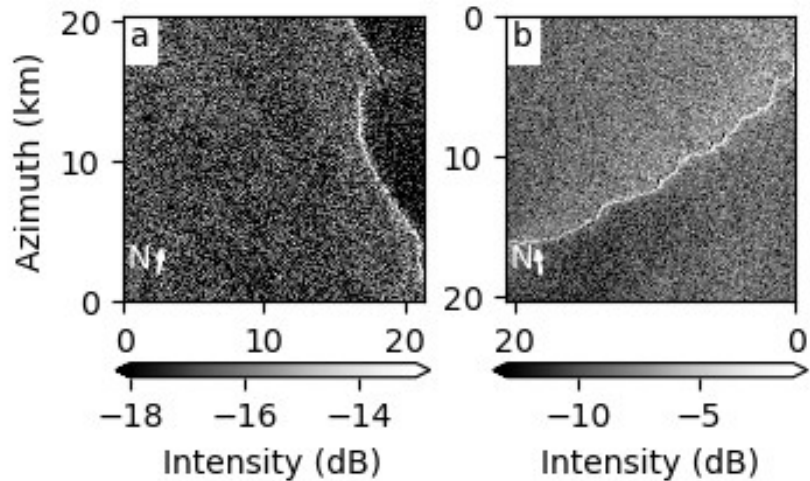
python  
powered

#090 / lon=-128.50 / lat=6.11 / inc=37.27



oceandatalab

# Back-scatter intensity

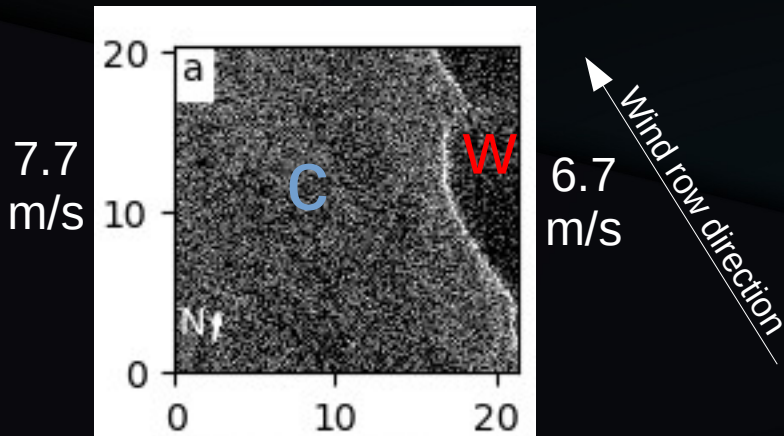


2016  
to  
2019

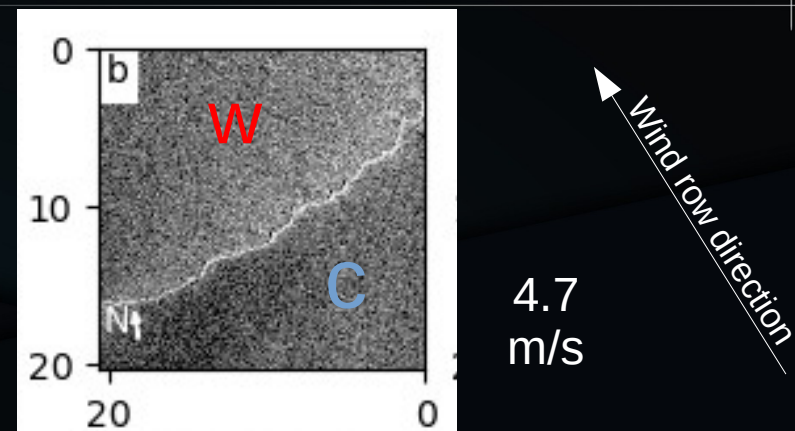
Back-scatter used  
in model to derive  
winds, much like  
scatterometer

LARGE SCALES  
Color – SST  
(Modis - NASA)  
Black – winds  
(MetOp scatterometer - Eumetsat)  
White – currents  
(altimetry assimilated  
into Mercator model)

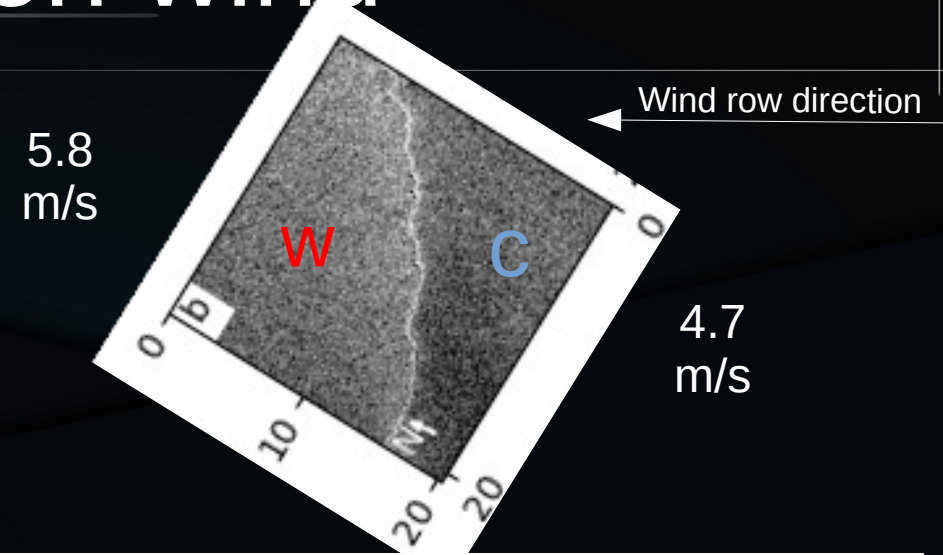
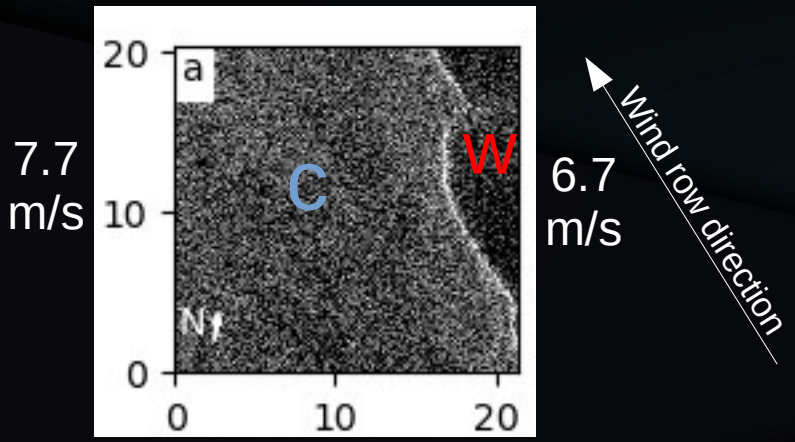
# Temperature impact on wind



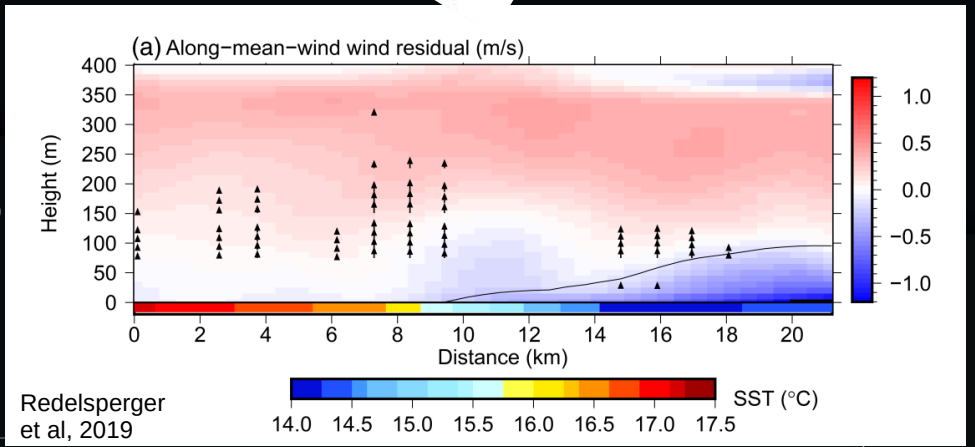
5.8 m/s



# Temperature impact on wind

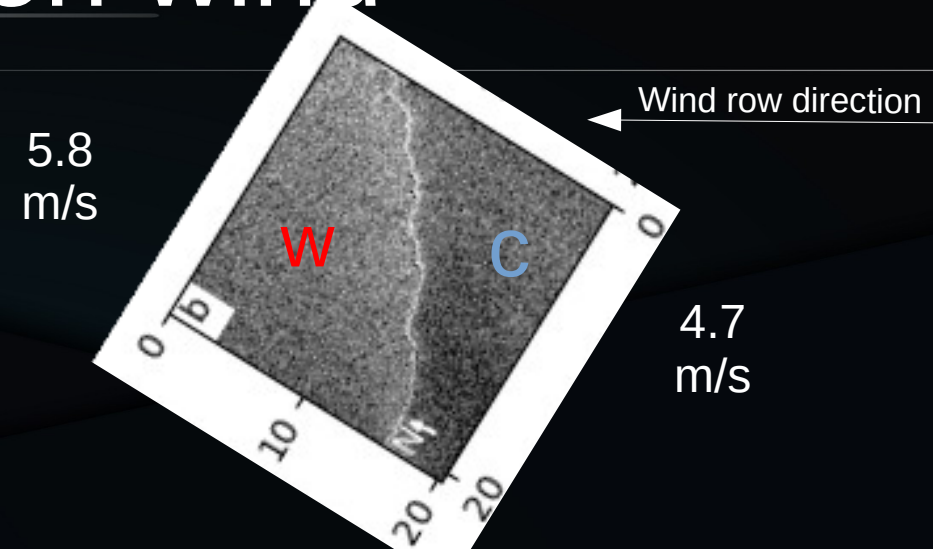
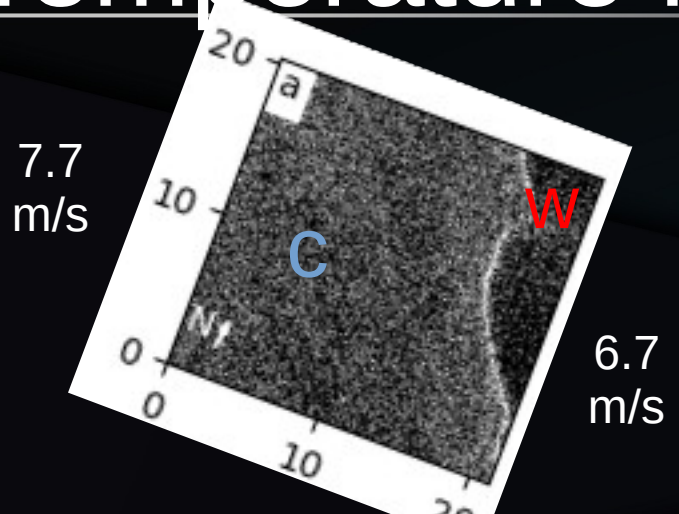


Cross-front winds  
Leading front

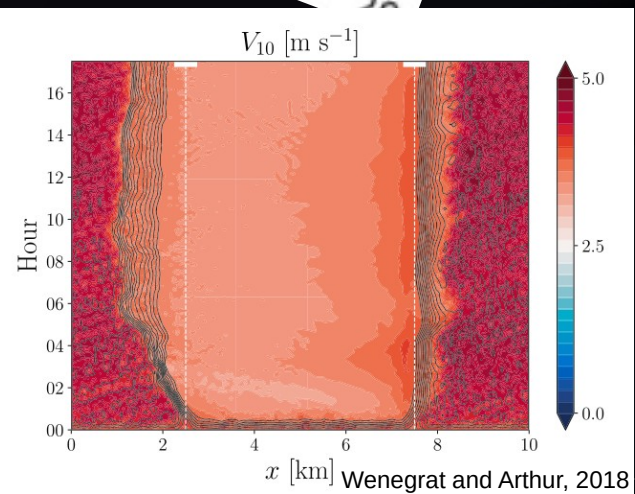




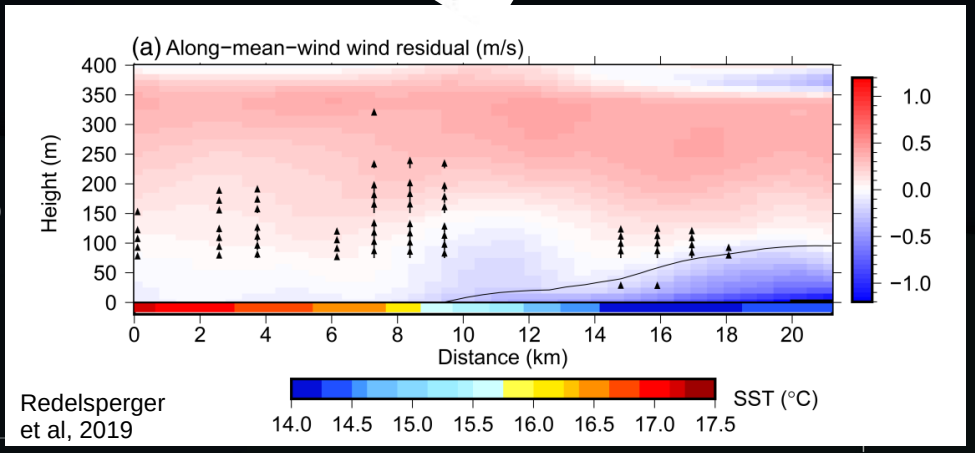
# Temperature impact on wind



Along-front winds  
Trailing front



Cross-front winds  
Leading front



# Wind relative to ocean surface instead of absolute wind affects backscatter!

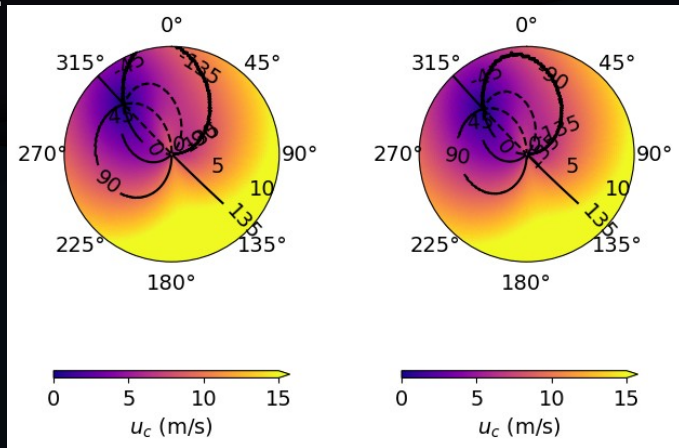
$$U_r(u_r, \theta_r) = U_w(u_w, \theta_w) - U_c(u_c, \theta_c)$$

Set by back-scatter →  $U_r$   
 Angle →  $\theta_r$   
 Radius →  $U_w$   
 Set by wind rows →  $\theta_w$   
 Color →  $U_c$   
 Contour →  $\theta_c$

Different current magnitudes and directions across the front could account for backscatter intensity difference

Bright, cold side:

- $U_w = 7.5 \text{ m/s}$
- $U_c = 0.8 \text{ m/s}$
- $\theta_c = -110^\circ$
- $\theta_r = -38^\circ$



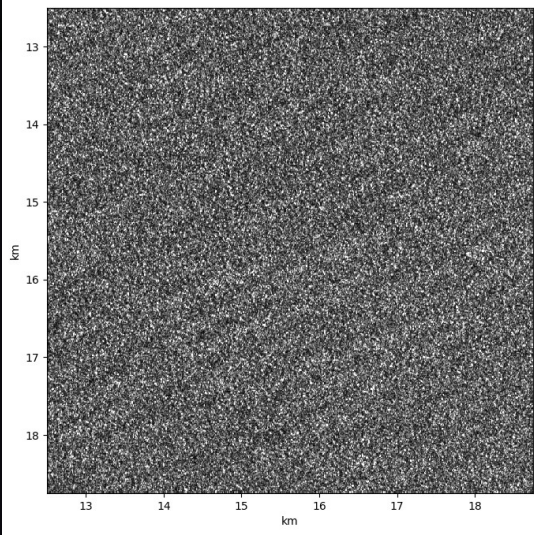
Dark, warm side:

- $U_w = 8 \text{ m/s}$
- $U_c = 1.3 \text{ m/s}$
- $\theta_c = -165^\circ$
- $\theta_r = -33^\circ$

But can that happen?

# Current inversion

Oct 1994



$$\omega_{obs} = \omega + \vec{k} \cdot \vec{u}$$

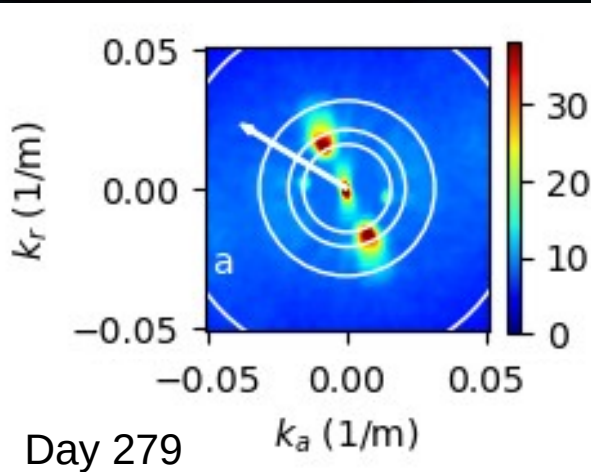
Observed frequency      Stationary frequency      Wave-number vector      Surface current

$$\frac{\partial \vec{k}}{\partial t} + \nabla \omega_{obs} = 0$$

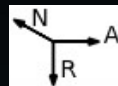
Conservation of crests

$$\omega_{obs} = constant = \sqrt{kg} + k_a u_a + k_r u_r$$

$$\mathbf{Ax} = \mathbf{b}$$



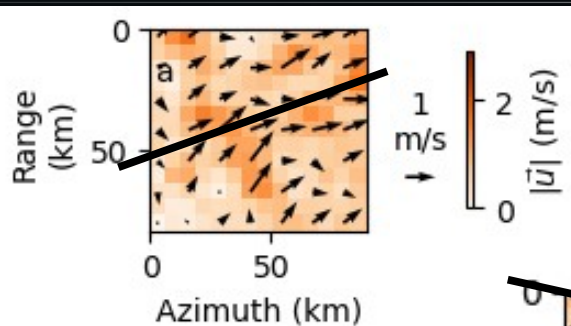
# Surface currents



Oct 1994

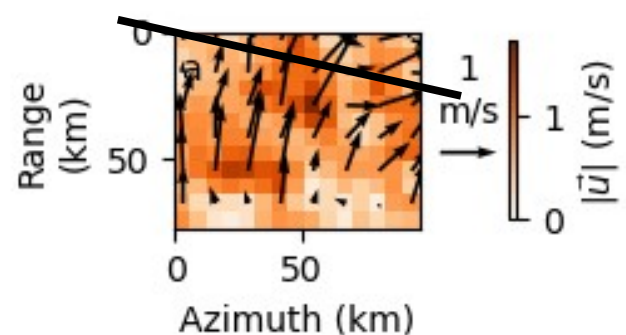
Along-front currents

Day 279



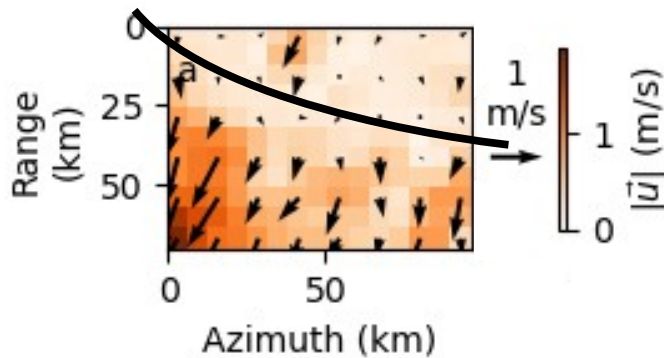
Across-front in N and along-front in S

Day 280



Across-front currents with strong cross-front divergent current

Day 282



# Conclusions

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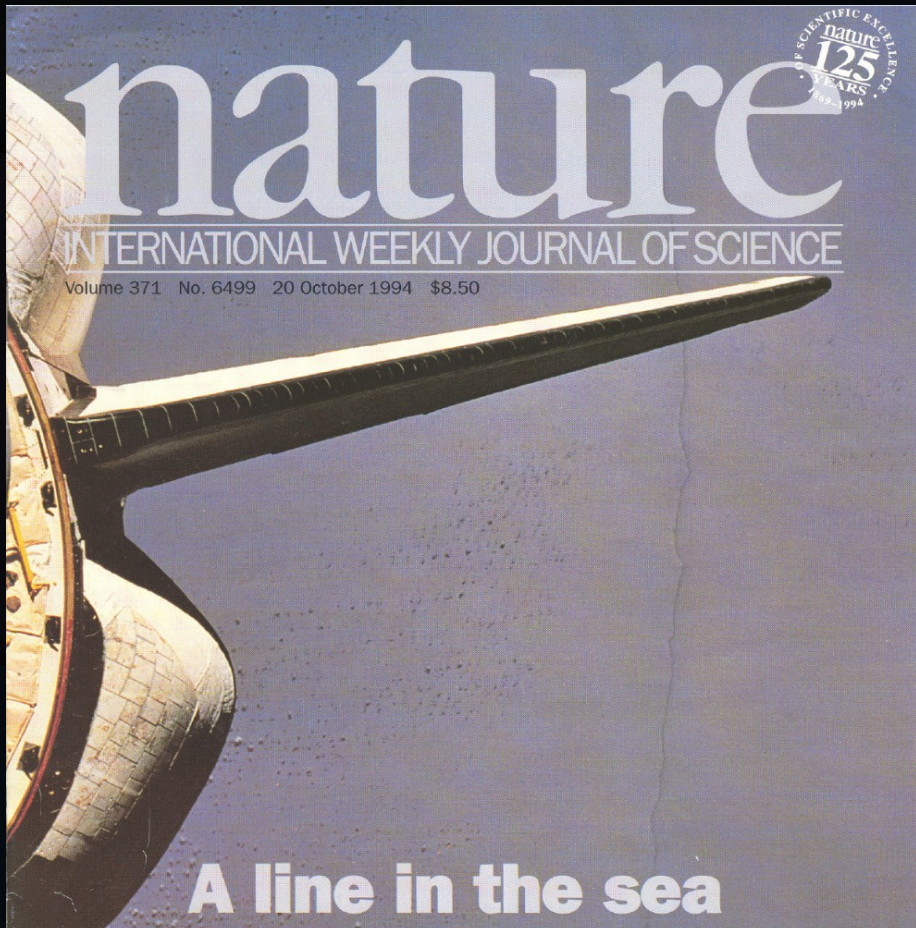
- Wind differences caused by SST differences across the front can explain back-scatter intensity differences across leading fronts
- On the trailing front, small variations in current magnitude and direction on the two sides of the front are important
- Surface currents can be any direction and strength around the front, but SAR data can determine what really happens



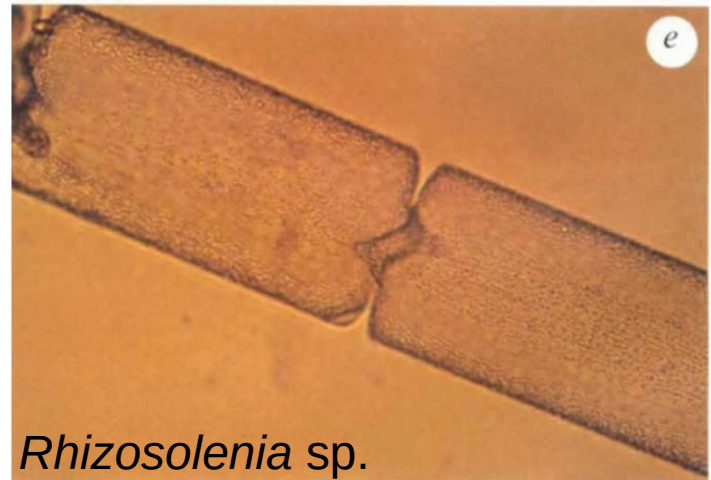
# Implications

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- Heat and energy analyses of TIVs can be incomplete
- Winds from scatterometer can be in error in regions of strong currents
- SAR offers opportunity to determine convergence and divergence from satellite



Questions?



Office of Naval Research, Department of Homeland Security, National Science Foundation, STEM Pre-Academy, Department of Oceanography

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Louis Marié, Fabrice Collard, Bertrand Chapron, Alexis Mouche

Anthony Kirincich, Ian Fernandez, Charina Repollo, Cesar Villanoy

Kristin Momohara, Lance Samura, Kellie Terada, Catalpa Kong

Alma, Angeles, Gabi, Sherry, Victoria; Kate

Bénédicte Dousset

My family

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Thank you

